## INJECTOR CALCULATIONS AT ORSAY

J. Gao

# CTF3 Injector Calculations at LAL/Orsay

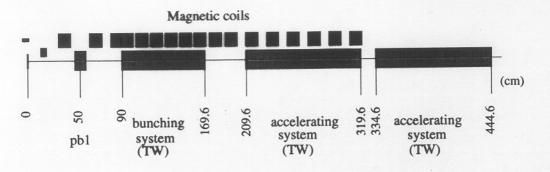
presented by J. Gao CERN, 26 Oct. 2000

- PARMELA simulations of the CTF3 injector (initial phase). Y. Thiery, J. Gao, and J. Le Duff
- Preliminary design of a TW buncher for CTF3

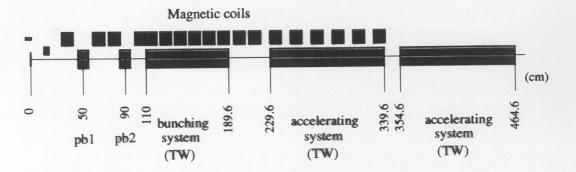
   (analytical design, Superfish, Urmel, HFSS).
   P. Avrakhov, J. Gao, and R. Raphael
- Analytical design of the waveguide-cavity coupling system used in TW buncher and the fully beam loaded accelerating structures. J. Gao

#### The layout of the injector of the initial stage of CTF3

#### case 1: one prebuncher



case 2: two prebunchers



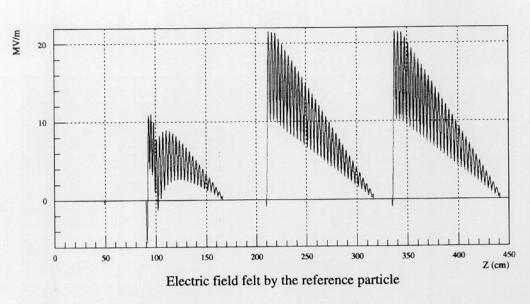
#### Results of the simulations

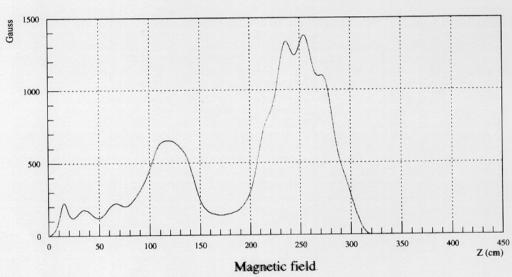
(Observation at the end of the second section)

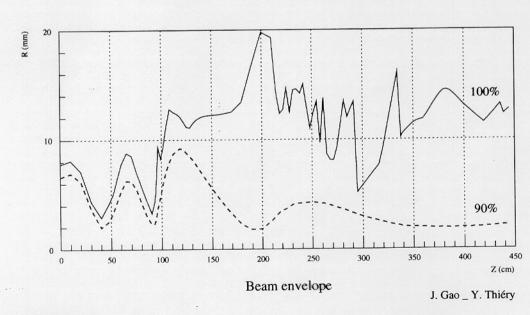
emited particle: 500		phi0±180°		Δphi=20°				
case	Z (cm)'	Nbp :	W (MeV)	Nbp	Exrms (mm_mrad)	Eyrms (mm_mrad)	Phirms (deg)	Wrms (MeV)
one prebuncher	444.56	423	22.63	372	37.23	25.99	4.385	0.2362
two prebunchers	464.56	462	22.67	429	23.16	24.04	3.599	0.1679

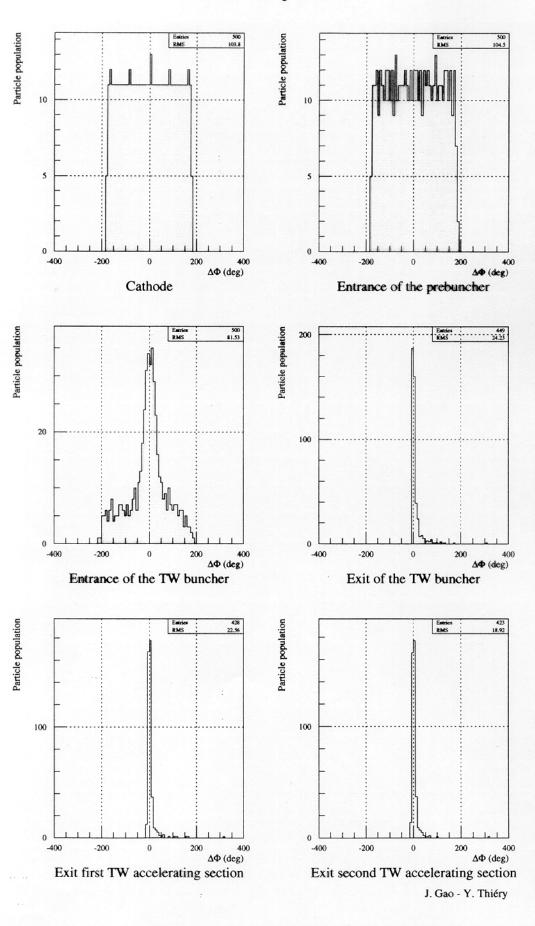
J. Gao - Y. Thiéry

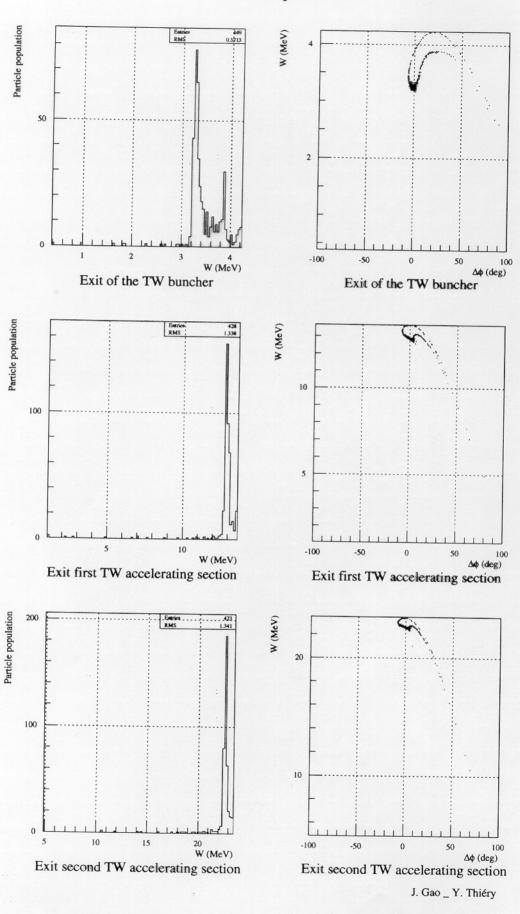
case 1: one prebuncher

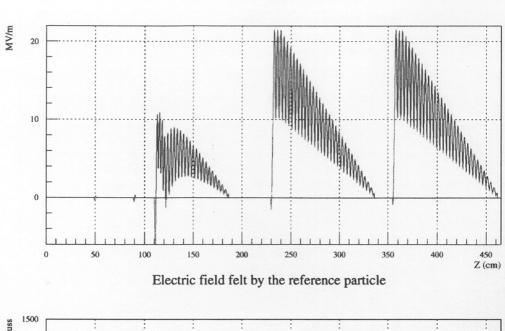


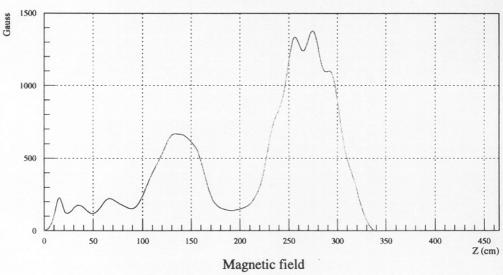


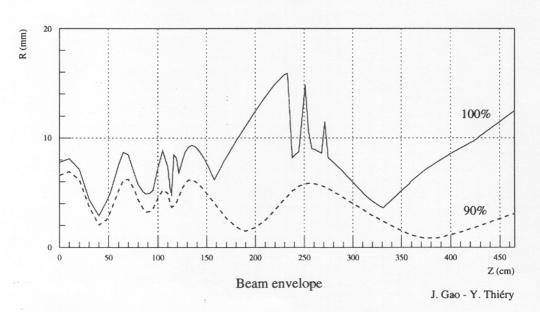


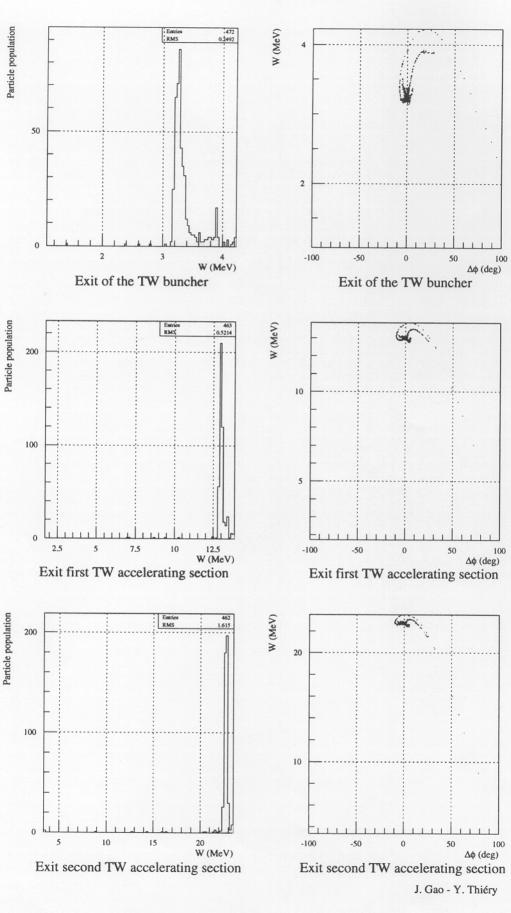


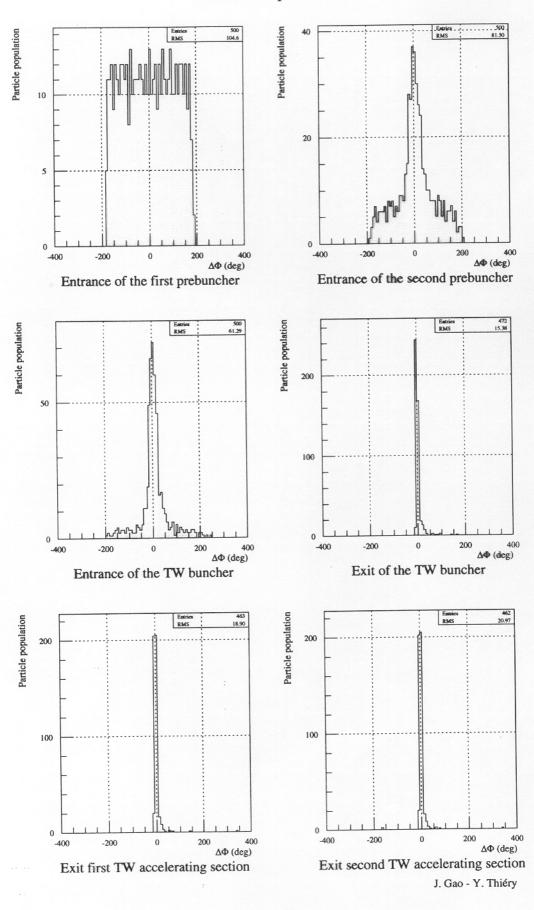












#### Results of the simulations CTF3

#### case two prebunchers

(Observation at the end of the second section)

emited p		phi0:	±180°	Δphi=20° (±10°)				
W0 (MeV)	Z (cm)	Nbp	W (MeV)	Nbp	Exrms (mm_mrad)	Eyrms (mm_mrad)	Phirms (deg)	Wrms (MeV)
0.135	464.56	430	22.64	358	22.73	21.80	3.454	0.1909
0.140	464.56	462	22.67	429	23.16	24.04	3.599	0.1679
0.145	464.56	466	22.76	383	29.17	27.93	2.510	0.1295

J. Gao - Y. Thiéry

### Simulation of TW buncher for CTF3

P. Avrakhov\* LAL, Orsay

#### Introduction

The simulations results of a high current bunching structure for CLIC [1] Test Facility (CTF3) drive beam are given. The report consists of choosing cavity dimensions and numerical simulations. These results were obtained by using URMEL, SLANS and Ansoft HFSS.

## Complex disk-loaded bunching structure

The TW bunching structure for CTF3 [2] drive beam has two kinds of cells with phase velocities  $\beta$ =0.75 and  $\beta$ =1 [3]. The initial part of this cavity has 4 cells with phase velocity 0.75c for frequency 2998 MHz on working mode  $2\pi/3$ . The second part of the cavity has 24 cells with phase velocity equal the speed of light for the same frequency and working mode.

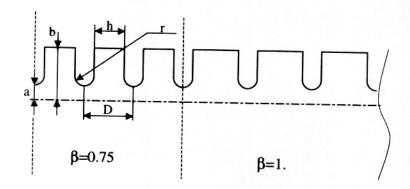


Figure 1. Disk loaded bunching structure with two kind of cells of  $\beta=0.75$  and  $\beta=1$ .

The initial analytical estimation of the TW buncher cells dimensions is given in Table 1.

Cell type	D (mm)	h (mm)	a (mm)	b (mm)	r(mm)	v <sub>o</sub> /c
β=0.75	25	13.7	14.6	40	5.5	0.031
β=1	33	20	16	40	6.6	0.029

Table 1. Preliminary dimensions of the buncher.

In numerical simulations were kept frequency, period D and group velocity  $v_g$  of each part of the buncher.

visitor from BINP, Protvino, Russia

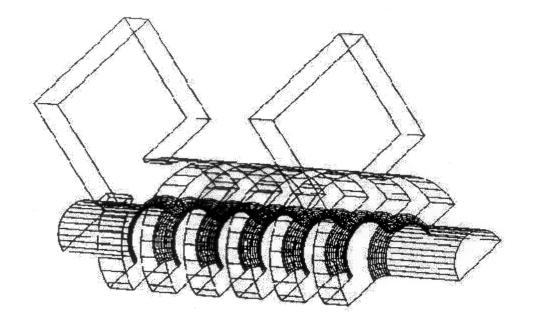


Figure 3. HFSS geometry of a 6-cells model for matching TW buncher coupler cavity.

waveguides. Eigen mode simulations by HFSS shows often big differences with drive solution of the same geometry. A few examples of the drive solutions for this system are given in Figures 6-12.

For the identification of modes real part and phase of electric field on the axis of this model were examined. Figures 4, 5 show the behavior of the electric field and the phase variation for  $2\pi/3$  mode. Table 7 and 8 summarize the results for 6-cells model of the first part ( $\beta$ =0.75) and the second part ( $\beta$ =1) of the TW buncher.

Width of coupling slot (mm)	Frequency of 2π/3 mode (MHz)	VSWR on 2π/3 mode frequency
20	2978.8	1.33
30	3008	1.43
35	3005.6	1.02
40	3004.1	1.005

Table 7. HFSS simulation results for the 6-cells model of the first part of the TW buncher with  $\beta$ =0.75

Width of coupling slot (mm)	Frequency of $2\pi/3$ mode (MHz)	VSWR on 2π/3 mode frequency
20	2994.2	1.04
30	2997.7	1.02
40	2992.4	1.007

Table 8. HFSS simulation results for the 6-cells model of the second part of the TW buncher with  $\beta=1$ 

#### Summary of the URMEL simulations

The URMEL simulation for the first part of buncher with  $\beta$ =0.75 is given in Table 2.

Cell type	D (mm)	h (mm)	a (mm)	b (mm)	$v_g/c$
β=0.75	25.	14.	17.	43.41	0.0312

Table 2. The URMEL simulation results for the first part of the buncher ( $\beta$ =0.75) .

Table 3. shows few points of dispersion curves of the first part of the buncher for fundamental and lowest dipole modes.

Mode	Fundamental	Dipole
0	2889.97	4105.17
π/6	2900.76	4044.71
π/3	2929.07	3964.59
π/2	2965.09	3912.40
2π/3	2998.30	3883.29
5π/6	3020.99	3869.10
π	3028.98	3864.89

Table 3. Points of the lowest dispersion curves for the first part of the buncher ( $\beta$ =0.75).

Tables 4 and 5 summarize the same parameters for the second part of the buncher with  $\beta=1$ .

Cell type	D (mm)	h (mm)	a (mm)	b (mm)	$v_g/c$
β=1	33.2	20.	16.8	42.42	0.0295

Table 4. The URMEL simulation results for the second part of the buncher ( $\beta=1$ ).

Mode	Fundamental (MHz)	Dipole (MHz)
0	2923.16	4213.01
π/6	2930.06	4132.75
π/3	2948.61	4060.73
π/2	2973.48	4016.55
2π/3	2997.76	3991.26
5π/6	3015.20	3978.59
π	3021.51	3974.78

Table 5. Points of the lowest dispersion curves for the second part of the buncher  $(\beta=1)$ .

#### Summary of the HFSS simulations

3-D simulation of the waveguide cavity coupling system of the buncher was produced by using Ansoft HFSS. At first the frequencies of input and output cells are adjusted. It means eigen frequency of the input cell with perfectly loaded waveguide (See Figure 2) equals eigen frequency of intermediate cells of the buncher. The first (phase velocity  $\beta$ =0.75) part and the second ( $\beta$ =1) part of the TW buncher was matched separately.

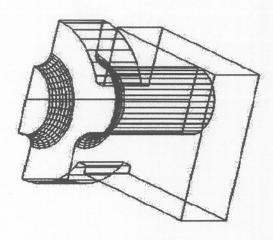


Figure 2. Half of input buncher cell with loaded waveguide

The heights of both waveguides are equal to heights of coupler cells. The distance between axis of the cells and touched inner wall of the waveguide is equal to radius of the coupler cells. Table 6 represents new dimensions of the input cells of the buncher for different width of a coupling slot between the coupler cell and the waveguide.

		.,	,
Cor	upling slot	Radius of input cells (mm)	Radius of input cells (mm)
wi	dth (mm)	for the part with $\beta$ =0.75	for the part with $\beta=1$
	20	43.34	42.6
	30	-	41.2
	35	41.92	-
	40	41.08	40.2
	50	39.4	-

Table 6. Cell radius of matching input vs coupling slot width.

For the matching of the waveguide coupler to the TW buncher a 6-cells model was used (See Figure 3). The HFSS simulation doesn't provide accurate simulation results in this case. It is explained probably by a high level storage energy on eigen modes in this resonance structure compare with drive energy in

#### Concluding remarks

For more accurate definition of the coupler dimensions an experimental test or another RF code calculation can be used. In addition the accelerating field distribution in the proposed structure should be computed and adjusted.

#### Acknowledgments

I thank J. Gao and J. Le Duff for providing useful information and discussions. P. Lepercq and B. Mouton helped me in computer utilization.

#### References

- [1] H. Braun and 10 co-authors, "CLIC A compact and Efficient High Energy Linear Collider", PAC95, Dallas, May 1995
- [2] CLIC study team, "Proposals for future CLIC studies and a new CLIC test facility (CTF3)", CLIC Note 402
- [3] Y. Thiery, J. Gao and J. Le Duff, "Design studies for high current bunching system for CLIC test facility (CTF3) drive beam", Note LAL-SERA-2000-130, CERN, May 2-3, 2000

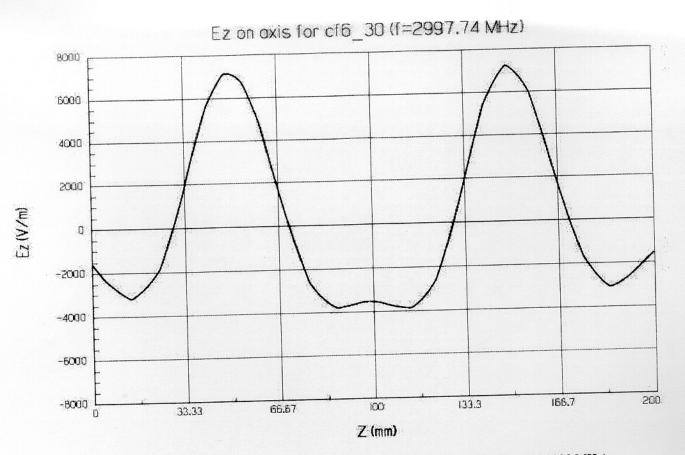


Figure 4. Distribution of Ez on axis for 6-cells model with  $\beta$ =1 (slot=30x20, f=2998 MHz)

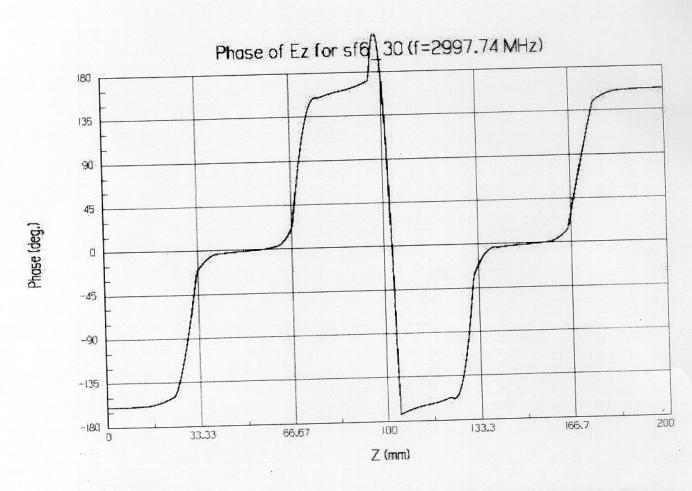
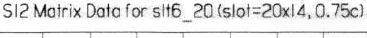


Figure 5. Ez phase distribution on axis for 6-cells model with  $\beta$ =1 (slot=30x20, f=2998 MHz)





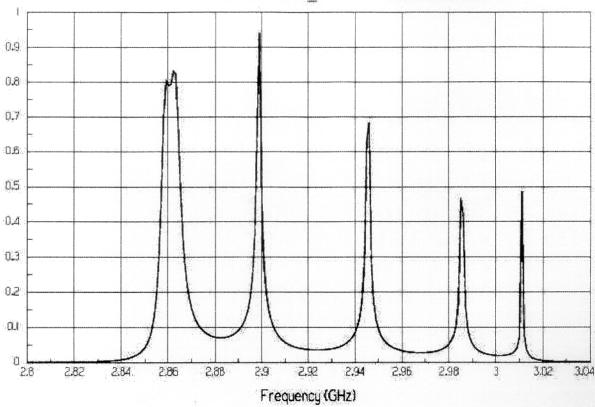


Figure 6. Fundamental mode passband for 6-cells model with β=0.75, slot=20x14

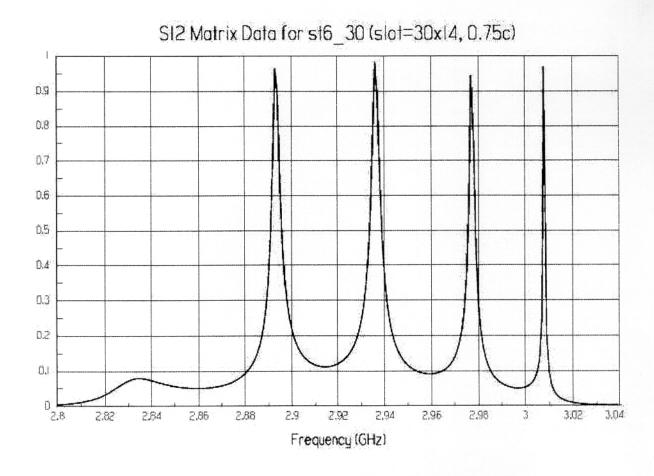


Figure 7. Fundamental mode passband for 6-cells model with  $\beta$ =0.75, slot=30x14

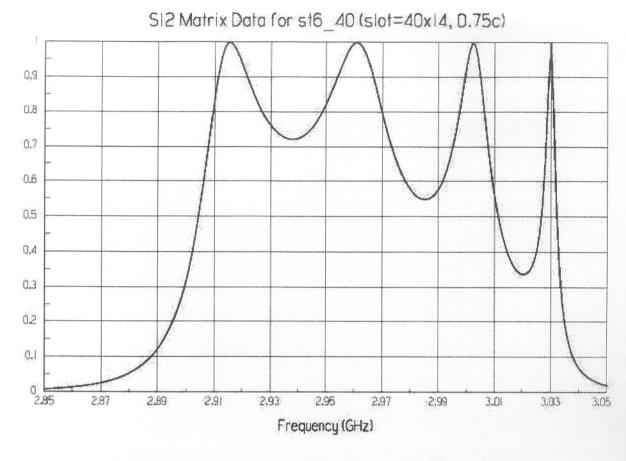


Figure 8. Fundamental mode passband for 6-cells model with β=0.75, slot=40x14

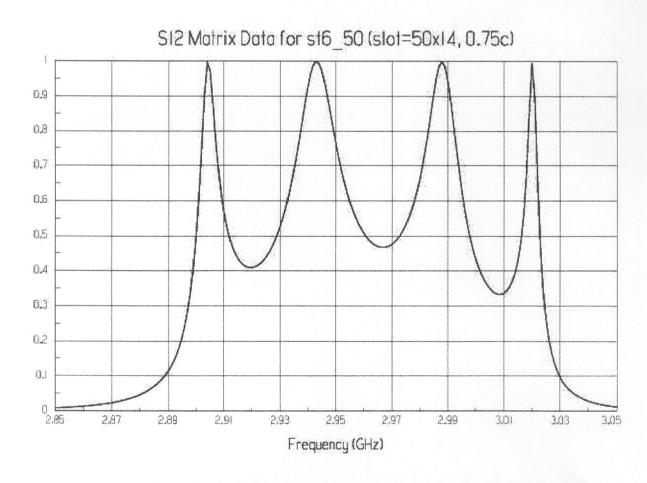
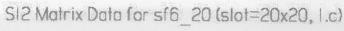


Figure 9. Fundamental mode passband for 6-cells model with  $\beta$ =0.75, slot=50x14



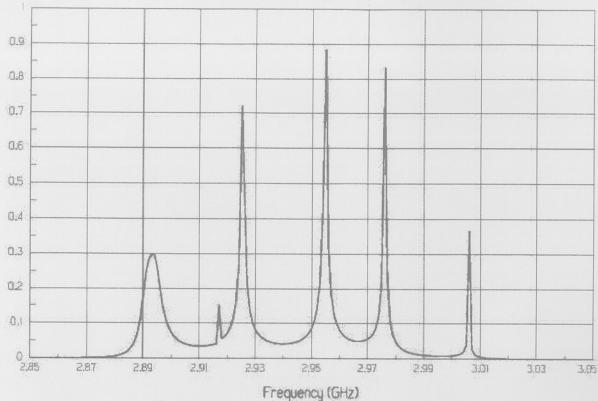


Figure 10. Fundamental mode passband for 6-cells model with  $\beta$ =1, slot=20x20

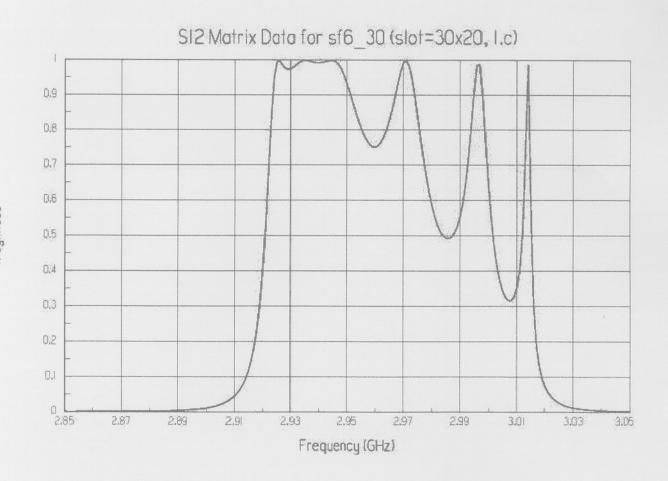


Figure 11. Fundamental mode passband for 6-cells model with  $\beta$ =1, slot=30x20

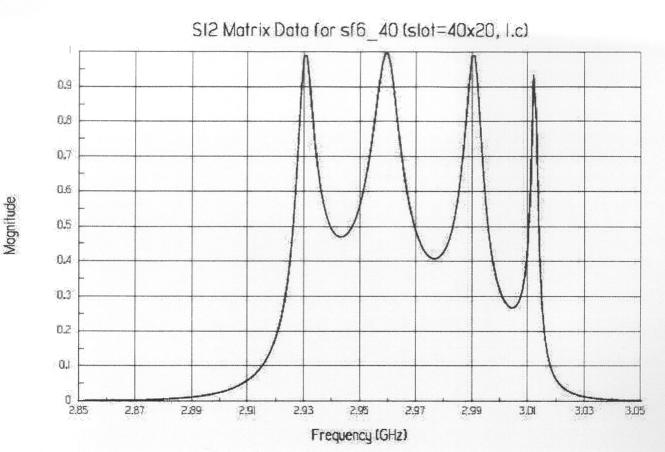


Figure 12. Fundamental mode passband for 6-cells model with  $\beta$ =1, slot=40x20

# Analytical Determination of the Coupling Coefficient of a Waveguide Cavity Coupling System

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#### Abstract

By applying the perturbation method, we show in a general way how to determine the coupling coefficient of a waveguide cavity coupling system and as a special example we derive the analytical expressions of the coupling coefficient for a waveguide-cavity coupling system as shown in Fig. 1. The term "cavity" in this paper stands for the cavity in both standing wave and traveling wave structures.

#### 1 Introduction

In the design and construction of klystrons and linear accelerating structures the coupling systems shown in Fig. 1 [1][2] and Fig. 2 are the most frequently used ones. The cavities can be standing wave or traveling wave ones. To determine the coupling coefficient between the waveguide and the cavity one can use different methods such as experiments, numerical simulations, and analytical calculations. In this paper we will concentrate on the coupling system shown in Fig. 1. The analytical treatment for the coupling system shown in Fig. 2 has been given in refs. [3] and [4].

#### 2 General theory

In a rectangular waveguide of width a and height b the normalized  $H_{nm}$  modes can be derived from the scalar function [5]:

$$\psi_{nm}(x,y) = \left(\frac{\epsilon_{0n}\epsilon_{0m}}{abjk_0 Z_0 \Gamma_{nm} k_{c,nm}^2}\right)^{1/2} \cos\left(\frac{n\pi}{a}\right) \cos\left(m\pi \frac{2y-b}{b}\right)$$
(1)

according to the following relations:

$$\mathbf{h}_{znm} = \mathbf{a}_z k_{cnm}^2 \psi_{nm} \tag{2}$$

$$\mathbf{h}_{nm} = -\Gamma_{nm} \nabla_t \psi_{nm} \tag{3}$$

$$\mathbf{e}_{nm} = \frac{jk_0Z_0}{\Gamma_{nm}}(\mathbf{a}_x\mathbf{a}_y - \mathbf{a}_y\mathbf{a}_x) \cdot \mathbf{h}_{nm} \tag{4}$$

$$\mathbf{E}_{nm}^{\pm} = \mathbf{e}_{nm} e^{\mp \Gamma_{nm}z} \cdot \mathbf{h}_{nm} \tag{5}$$

$$\mathbf{H}_{nm}^{\pm} = (\pm \mathbf{h}_{nm} + \mathbf{h}_{znm})e^{\mp \Gamma_{nm}z} \tag{6}$$

where  $\epsilon_{0n} = 1(n=0)$  and  $\epsilon_{0n} = 2(n>0)$ ,  $Z_0 = 120\pi(\Omega)$ ,  $k_{c,nm}^2 = (m\pi/b)^2 + (n\pi/a)^2 - k_0^2$ ,  $\mathbf{h}_{nm}$  and  $\mathbf{e}_{nm}$  are the transverse magnetic and electric normal mode fields,  $\Gamma_{nm}^2 = k_{c,nm}^2 - k_0^2$ ,  $k_0 = 2\pi/\lambda$ , and the  $\lambda$  is the wavelength in free space. The normalization in eq. 1 has been chosen so that

$$\int_{0}^{a} \int_{0}^{b} \mathbf{e}_{nm} \times \mathbf{h}_{nm} \cdot \mathbf{a}_{z} dx dy = 1 \tag{7}$$

Now we consider the case (see Fig. 3) of a waveguide excited by an aperture (see Fig. 4) which can be equivalent to an electric dipole **P** and a magnetic dipole **M**. The scattered field can be expanded in terms of the normal waveguide modes as follows [5]:

$$\mathbf{E}_s = \sum a_n \mathbf{E}_n^+ \qquad z > 0 \tag{8}$$

$$\mathbf{H}_s = \sum a_n \mathbf{H}_n^+ \qquad z > 0 \tag{9}$$

$$\mathbf{E}_{s} = \sum b_{n} \mathbf{E}_{n}^{-} \qquad z < 0 \tag{10}$$

$$\mathbf{H}_s = \sum b_n \mathbf{H}_n^- \qquad z < 0 \tag{11}$$

where the expansion coefficients  $a_n$  and  $b_n$  can be obtained by the following relations [5]:  $2a_n = j\omega(\mu_0 \mathbf{H}_n^- \cdot \mathbf{M} - \mathbf{E}_n^- \cdot \mathbf{P})$ 

$$2a_{n} = j\omega(\mu_{0}\mathbf{H}_{n}^{-} \cdot \mathbf{M} - \mathbf{E}_{n}^{-} \cdot \mathbf{P})$$

$$2b_{n} = j\omega(\mu_{0}\mathbf{H}_{n}^{+} \cdot \mathbf{M} - \mathbf{E}_{n}^{+} \cdot \mathbf{P})$$

$$(12)$$

$$2b_n = j\omega(\mu_0 \mathbf{H}_n^+ \cdot \mathbf{M} - \mathbf{E}_n^+ \cdot \mathbf{P})$$
 (13)  
electric and magnetic dipoles can be estimated as follows

where  $\omega = \frac{k_{10}}{c}$ , the electric and magnetic dipoles can be estimated as follows [5]:

$$\mathbf{P} = -\frac{\pi l_1^3 (1 - e_0^2)}{3E_0(e_0)} \epsilon_0 \mathbf{E}_0 \tag{14}$$

(17)

(21)

$$\mathbf{M}_1 = \frac{\pi l_1^3 e_0^2}{3(K(e_0) - E_0(e_0))} \mu_0 \mathbf{H}_1$$
 (15)

$$\mathbf{M}_{2} = -\frac{\pi l_{1}^{3} e_{0}^{2} (1 - e_{0}^{2})}{3(E_{0}(e_{0}) - (1 - e_{0}^{2}) K(e_{0}))} \mu_{0} \mathbf{H}_{2}$$
(16)

$$K(e_0) = \frac{\pi}{2} \left( 1 + \left(\frac{1}{2}\right)^2 e_0^2 + \left(\frac{1 \cdot 3}{2 \cdot 4}\right)^2 e_0^4 + \left(\frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6}\right)^2 e_0^6 + \cdots \right)$$
(16)

$$E(e_0) = \frac{\pi}{2} \left( 1 - \left(\frac{1}{2}\right)^2 e_0^2 - \left(\frac{1 \cdot 3}{2 \cdot 4}\right)^2 \frac{e_0^4}{3} - \left(\frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6}\right)^2 \frac{e_0^6}{5} - \cdots \right)$$

$$e_0 = \left( 1 - \frac{l_2^2}{l_1^2} \right)^{1/2}$$

$$(19)$$

where  $\epsilon_0$  is the permittivity of the vacuum, and  $\mu_0$  is the permeability of the vacuum. When the aperture is circular of radius r, eqs. 14 and 15 can be simplified as follows:

$$\mathbf{P} = -\frac{2}{3}r^{3}\epsilon_{0}\mathbf{E}_{0}$$

$$\mathbf{M}_{1,2} = \frac{4}{3}r^{3}\mu_{0}\mathbf{H}_{1,2}$$
(20)

As a special example we consider the 
$$H_{10}$$
 mode in the waveguide. The normalized mode functions for the  $H_{10}$  mode are:

normalized mode functions for the  $H_{10}$  mode are:

$$\mathbf{E}_{10}^{+} = \mathbf{e}_{10}e^{-\Gamma_{10}z} \tag{22}$$

$$\mathbf{E}_{10}^{-} = \mathbf{e}_{10} e^{\Gamma_{10} z} \tag{23}$$

$$\mathbf{H}_{10}^{+} = (\mathbf{h}_{10} + \mathbf{h}_{z10})e^{-\Gamma_{10}z} \tag{24}$$

3

$$\mathbf{H}_{10}^{-} = (-\mathbf{h}_{10} + \mathbf{h}_{z10})e^{\Gamma_{10}z} \tag{25}$$

$$\mathbf{e}_{10} = -jk_0 Z_0 \left(\frac{2}{iabk_0 Z_0 \Gamma_{10}}\right)^{1/2} \sin\left(\frac{\pi x}{a}\right) \mathbf{a}_y \tag{26}$$

$$\mathbf{h}_{10} = \Gamma_{10} \left( \frac{2}{iabk_0 Z_0 \Gamma_{10}} \right)^{1/2} \sin \left( \frac{\pi x}{a} \right) \mathbf{a}_x \tag{27}$$

$$\mathbf{h}_{z10} = \left(\frac{2}{jabk_0 Z_0 \Gamma_{10}}\right)^{1/2} \frac{\pi}{a} \cos\left(\frac{\pi x}{a}\right) \mathbf{a}_z \tag{28}$$

$$\Gamma_{10} = k_0 \left( 1 - \left( \frac{\lambda}{2a} \right)^2 \right)^{1/2} \tag{29}$$

The peak power of the  $H_{10}$  mode inside the waveguide can be expressed as:

$$P_{max} = \frac{abZ_0k_0}{4\Gamma_{10}}H_{x,10,max}^2 \tag{30}$$

$$H_{x,10,max} = \frac{a\Gamma_{10}}{\pi} H_{z,10,max}$$
 (31)

where  $H_{x,10,max}$  and  $H_{z,10,max}$  are the peak magnetic fields of the  $H_{10}$  mode in the x and z directions, respectively. If on the surface of the dipole there is only magnetic field, the expansion coefficients  $a_1$  and  $b_1$  corresponding to  $H_{10}$  mode can be found from eqs. 12 and 13 as follows:

$$2a_1 = j\omega\mu_0 \mathbf{H}_{10}^- \cdot \mathbf{M} = j\omega\mu_0 \mathbf{h}_{z10} \cdot \mathbf{M}$$
 (32)

$$2b_1 = j\omega\mu_0 \mathbf{H}_{10}^+ \cdot \mathbf{M} = j\omega\mu_0 \mathbf{h}_{z10} \cdot \mathbf{M} = 2a_1$$
 (33)

With the above preparation one can start to establish the analytical formulae of the coupling coefficient of the waveguide-cavity coupling system shown in Fig. 1. According to the definition one has

$$\beta = \frac{P}{P_0^*} \tag{34}$$

where P is the power radiated into the waveguide from the cavity through the coupling aperture,  $P_0^* = P_0 + Uv_g/h$ ,  $P_0$  is the power dissipated on the coupler cavity wall, U is the energy stored inside the coupler cavity, and  $v_g$  is the group velocity of the structure (the case of  $v_g = 0$  corresponds to standing wave cavity). By using eqs. 30 and 34 one finds:

$$\beta = \frac{\pi^2 N Z_0 k_0 \Gamma_{10} e_0^4 l_1^6 e^{-2\alpha d} \sin^2\left(\frac{2\pi L}{\lambda_g}\right)}{9ab(K(e_0) - E(e_0))^2} \left(\frac{\pi}{a \Gamma_{10}}\right)^2 \frac{H_1^2}{P_0^*}$$
(35)

where N is the number of the waveguides connected to the coupler cavity (assuming that the magnetic field on each coupling aperture is the same),  $H_1$  is magnetic field at the location of the coupling aperture before the aperture is opened,  $\lambda_g$  is the waveguide wavelength of the  $H_{10}$  mode, d is the average wall thickness between the inner surface of the waveguide and the inner surface of the coupler cavity, and  $\alpha$  is the attenuation coefficient which can be expressed as  $\alpha = \frac{2\pi}{\lambda} ((\frac{\lambda}{4l_{1,2}})^2 - 1)^{1/2}$  depending on the wave inside the aperture is  $H_{10}$  or  $H_{01}$  like. In fact eq. 35 can be further simplified:

$$\beta = \frac{N\pi Z_0 k k_{10} l_1^6 e_0^4 e^{-2\alpha d} \sin^2\left(\frac{2\pi L}{\lambda_g}\right)}{9abRR_s (R+h) (K(e_0) - E(e_0))^2 \left(1 + \frac{Z_0 R}{2R_s (R+h)} \left(\frac{v_g}{c}\right)\right)} \left(\frac{\pi}{a \Gamma_{10}}\right)^2$$
(36)

where  $R_s$  is the metal surface resistance. If the aperture is circular with radius r the attenuation coefficient should be expressed as  $\alpha = \frac{2\pi}{\lambda} \left( \left( \frac{\lambda}{3.41r} \right)^2 - 1 \right)^{1/2}$ .

As an numerical example of a travelling wave structure with h=0.02, R=0.04,  $v_g/c=0.03$ , a=0.072, b=0.072, b=0.1, b=0.1, b=0.1, b=0.0023, b=0.0

#### 3 Conclusions

In this paper we have shown in a general way how to establish the coupling coefficient between a waveguide and a cavity. This method can be used either for the fundamental mode or the higher order mode cases. As a special example we have established the analytical expression of the coupling coefficient for a system shown in Fig. 1.

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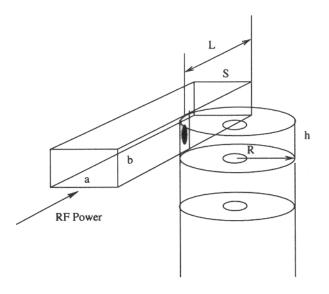


Figure 1: A waveguide cavity coupling system type I.

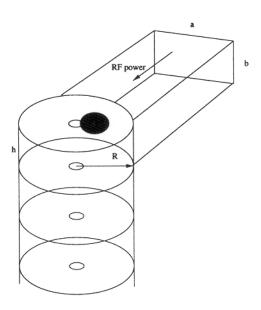


Figure 2: A waveguide cavity coupling system type II.

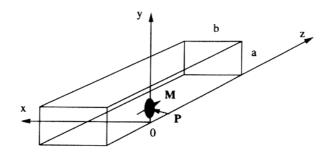


Figure 3: Waveguide excited by an electric dipole and a magnetic dipole.

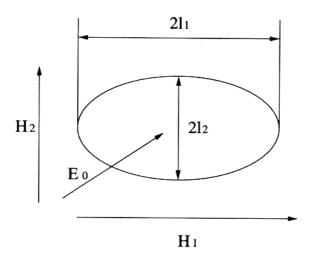


Figure 4: The elliptical coupling aperture with magnetic fields parallel to the surface and the electric field perpendicular to the surface.

# **Conclusions**

According to LAL-CTF3/CERN
 collabration program, a complete beam
 dynamics simulation for the CTF3 injector
 (initial phase) has been finished. For the
 two options (one and two prebunchers), the
 PARMELA simulation results show that
 they satisfy the required specifications.

- A preliminary design of the TW buncher has been started and is till going on.
- An analytical formula for the determination of the coupling coefficient of the waveguide-cavity coupling system used in the TW buncher and the fully beam-loaded accelerating structures has been established.

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